



Institut de



saclav

Fecherche sur les lois fondamentales de



# Magnetic braking and its effects during protostellar collapse

## When Magnetic Field leads to Catastrophe and Crisis

Patrick Hennebelle

Benoit Commerçon, Marc Joos, Jacques Masson, Andréa Ciardi Sébastien Fromang, Romain Teyssier, Philippe André, Gilles Chabrier

## Why *must* we understand collapse ?

Major astrophysical questions

### ⇒Determine the initial conditions of the protostars:

-entropy

-angular momentum (*the angular momentum problem*) -magnetic field (*the magnetic flux problem*)

## ⇒Binary and multiple system formation

## ⇒Disk formation: Planet formation and migration

## 1) Catastrophic braking

- **1.1) The catastrophe...**
- 1.2) Alleviating the catastrophe: magnetic configuration
- **1.3)** Alleviating the catastrophe: impact of turbulence
- **1.4)** Alleviating the catastrophe: non-ideal MHD ?
- **1.5)** Is there a catastrophe or was there a catastrophe?

### 2) Fragmentation crisis

- 2.1) A fragmentation "crisis" for low mass cores ?
- 2.2) How to solve it ?
- 2.3) Influence of B on high mass cores
- 2.4) When magnetic field and radiative feedback collaborate
- 2.5) A crisis: really ?

## Catastrophic braking 1.1) The catastrophe...

**1.2)** Alleviating the catastrophe: magnetic configuration

1.3) Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

300 AU



300 AU



300 AU



300 AU



300 AU















Can we understand this result by simple considerations ?

$$\frac{\rho V_{\theta}}{\tau_{br}} \propto B_z \frac{B_{\theta}}{4\pi h} \\ \frac{B_{\theta}}{\tau_{br}} \propto B_z \frac{V_{\theta}}{h} \\ \frac{B_{\theta}}{\tau_{br}} \propto B_z \frac{V_{\theta}}{h} \\ \frac{T_{rot}}{\tau_{rot}} \approx \frac{2\pi r_d}{V_{\theta}}, \\ \frac{\tau_{br}}{\tau_{rot}} \approx \frac{V_{\theta} \sqrt{4\pi h^2 \rho}}{2\pi r_d B_z} \\ V_{\theta} \approx \left(\frac{GM_d}{r_d}\right)^{1/2}, M_d \approx \pi r_d^{-2} z \rho \Rightarrow V_{\theta} \approx \left(G\pi \rho r_d z\right)^{1/2} \\ \Rightarrow \frac{\tau_{br}}{\tau_{rot}} \approx \left(\frac{z}{r_d}\right)^{1/2} \frac{G^{1/2} \rho}{B_z} \approx \left(\frac{z}{r_d}\right)^{1/2} \frac{\mu_{eff}}{(2\pi)^{1/2}}$$

 $z/r_d$  is easily < 10 while  $\mu_{eff}$  <  $\mu$  (as only a fraction of the column density has contracted)

Thus a value of  $\mu$ ~5-10 seems entirely reasonable.

#### **Can we understand this result by less simple considerations ?** Galli et al. 2006

Galli et al. study magnetized self-similar solutions and infer their asymptotic behavior. They show that because the field lines are strongly stretched by gravitational collapse, the field is strongly amplified and the braking very efficient.



Catastrophic braking
 1.1) The catastrophe...

#### 1.2) Alleviating the catastrophe: magnetic configuration

1.3) Alleviating the catastrophe: impact of turbulence1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

**Can different magnetic configurations modify magnetic braking ?** 





#### Joos et al. 2012

## Specific angular momentum above various density thresholds



Joos et al. 2012



and



, 24289 yr

200

400

r (AU)



1000

800

r (AU)

800

1000

400

200

Sonntag, 21. Oktober 12

Magnetic transport of angular momentum: radial component (cm<sup>2</sup> s<sup>-2</sup>)

## **Magnetic braking**

#### (Gillis et al. 74,79, Mouschovias & Paleologou 79,80, Basu & Mouschovias 95, Shu et al. 87)

rotation generates torsional Alfvén waves which carry angular momentum outwards

<u>Typical time:</u> AW propagate far enough so that the external medium receives angular momentum comparable to the cloud initial angular momentum

Magnetic field parallel to the rotation axis:

$$\rho_{core} Z_{core} \approx \rho_{env} \tau_{para} V_a$$
  

$$\Rightarrow \tau_{para} \approx (\rho_{core} / \rho_{env}) \times (Z_{core} / V_a)$$
  

$$\approx \frac{M}{\phi} \times \sqrt{\frac{\pi}{\rho_{env}}}$$
  
since  $M = 2\pi Z_{core} R^2 \rho_{core}$  and  $\phi = \pi R^2 B$ 



In the aligned configuration, the magnetic braking can be much more efficient if the field lines are fanning out (Mouschovias 1991)

$$M_{core}J_{core} \approx M_{env}J_{env}$$

$$\pi\rho_{core}Z_{core}R_{core}^{4}\omega_{core} \approx \pi\rho_{env}\tau_{para}V_{a}R_{env}^{4}\omega_{env}$$

$$\Rightarrow \tau_{para} \approx \frac{\rho_{core}}{\rho_{env}}\frac{Z_{core}}{V_{a}}\frac{R_{core}^{4}}{R_{env}^{4}}\frac{\omega_{core}}{\omega_{env}}$$

$$\approx \frac{M}{\phi} \times \sqrt{\frac{\pi}{\rho_{env}}}\frac{R_{core}^{2}}{R_{env}^{2}}$$
since  $M = 2\pi Z_{core}R_{core}^{2}\rho_{core}$  and  $\phi = \pi R_{env}^{2}B_{env}$ 
and assuming corotation  $\omega_{core} \approx \omega_{env}$ 

Thus, the magnetic braking is more efficient when field lines are fanning out

#### Magnetic braking in the perpendicular case

The geometry of the field lines is complex. It is traditionally assumed that  $B\alpha 1/R$  (Mouschovias 1991)

R

 $\rho_{ext}$ 

В

$$\pi \rho_{core} Z_{core} R_{core}^{4} \approx \pi \rho_{env} Z_{core} \left( R_{perp}^{4} - R_{core}^{4} \right)$$

$$\Rightarrow \tau_{perp} \approx \int_{R_{core}}^{R_{perp}} \frac{dR}{V_{a}} = \frac{R_{c}}{2V_{a}(R_{c})} \left( \sqrt{1 + \rho_{core} / \rho_{env}} - 1 \right)$$

$$\approx \frac{M}{\phi} \times 2 \sqrt{\frac{\pi}{\rho_{core}}}$$

since  $M = 2\pi Z_{core} R^2 \rho_{core}$  and  $\phi = \pi R^2 B$ 

**Comparison between timescales** 

(Joos et al. 2012)



when the field lines are aligned: => the braking is more efficient in the perpendicular case  $\frac{\tau_{perp}}{\tau_{max}} \approx \sqrt{\frac{\rho_{env}}{\rho}}$ When the field lines are aligned:

When the field lines are fanning out, assuming  $\rho \alpha R^{-2}$ => the braking is more efficient in the aligned case  $\frac{\tau_{perp}}{\tau_{name}} \approx \sqrt{\frac{\rho_{core}}{\rho_{emp}}}$ 





#### **Contribution of braking due to outflows**

Comparison between the mean flux of angular momentum due to magnetic braking and outflow at 150 AU above equatorial plane



## 1) Catastrophic braking

1.1) The catastrophe...

1.2) Alleviating the catastrophe: magnetic configuration

#### **1.3)** Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD?

1.5) Is there a catastrophe or was there a catastrophe?

2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?



## Another limitation: Impact of turbulence diffusion/reconnection

(Seifried et al. 2011, Santos-Lima et al. 2012)





Santos-Lima et al. 2012

10<sup>-2</sup> 10<sup>-1</sup> 10<sup>0</sup> 10<sup>1</sup> 10<sup>2</sup> 10<sup>3</sup> 10<sup>4</sup> 10<sup>5</sup> (1.4x10<sup>-19</sup> g cm<sup>-3</sup>)

#### Spontaneous symmetry breaking: the interchange instability



## Mass to flux ratio as a function of time for various initial magnetisation and level or turbulence



Seifried et al. 2012

Joos et al. 2013

#### Disk masses

## Mean flux along the pole and in the radial direction



⇒Turbulence reduces magnetic braking and disks tend to be bigger (for intermediate magnetic field)



## 1) Catastrophic braking

1.1) The catastrophe...

1.2) Alleviating the catastrophe: magnetic configuration

**1.3) Alleviating the catastrophe: impact of turbulence** 

#### 1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

#### **Detailed microphysics implying chemistry network**



#### **Can ambipolar diffusion modify this?**

(Mellon & Li 2009, Duffin & Pudritz 2009)



#### Impact of ohmic dissipation (a solution to the flux problem ?)

Interestingly: Desh and Mouschovias, Nakano et al. (2002) predicts that a lot of flux should be lost at densities larger than  $10^{11}$  cm<sup>-3</sup>(grains carry the charge).

First calculation with resistive MHD done by Machida et al. 2007 Characteristic scales of about 10-20 AU ⇒Formation of compact disks

Dapp & Basu recent work (1D calculation)





#### **Resistive 3D simulations, aligned case** (Machida et al. 2011) Growth of the disk



### **Resistive 3D simulations, aligned case** (Machida et al. 2011) Comparison between different models.



However, Li et al. 2011 performed a series of simulations taking into account ambipolar diffusion, Hall effect and Ohmic dissipation and find no disk at all...



### **Confused situation**

Could be due to: -Li et al. have a sink whose radius is 6AU -Machida et al. perform 3D non-axisymmetric runs while Li et al. perform 2D runs. Possibly due to enhanced transport/flux lost in Machida et al. ?

## 1) Catastrophic braking

1.1) The catastrophe...

1.2) Alleviating the catastrophe: magnetic configuration

**1.3) Alleviating the catastrophe: impact of turbulence** 

**1.4) Alleviating the catastrophe: non-ideal MHD ?** 

#### **1.5)** Is there a catastrophe or was there a catastrophe ?

#### 2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

#### Are there disks at the class 0 stage ?

#### Difficult issue because strong emission from the envelope that must be removed.

-Jorgensen et al. claim to infer disks from their modeling (disk is not resolved) but Brinch et al. (2009) do not see rotation in some of them

-Enoch et al. (2009) claim to resolve a 1 Ms disk in a 8 Ms source but conclusion depends on assumptions (density profile) for the envelope



### **Comparison of the PdBI maps with MHD simulations**

Hydrodynamical simulations produce too much extended (+ multiple) structures if compared to Maury et al. 2010 Observations.

 $\Rightarrow$  MHD simulations ?

MHD simulations : produce PdB-A synthetic images with **typical FWHM ~ 0.2" - 0.6"** 

Similar to Class 0 PdB-A sources observed !

need B to produce compact, single PdB-A sources.



Maury et al. 2010

An alternative view: Stamatellos et al. (2010) propose that massive disks form and quickly fragment. Thus the chance to see them is weak.



#### Some conclusions regarding disk formation and braking:

-magnetic field modifies very significantly the early disk formation

-for intermediate magnetization, the geometry is important and braking is more efficient in the aligned case

-turbulence is reducing the braking because it diffuses the field and naturally generates non-aligned configuration, it helps forming disks

-non-ideal MHD may help but some debate remains. It seems reasonable that it should help forming small disk

-Unclear that there is a *problem* since very few observations of class 0 disks are available

-We need to get a distribution of inner structure and of initial conditions (field strength and configuration, rotation) before we can conclude whether the problem is understood Catastrophic braking
 1.1) The catastrophe...

**1.2)** Alleviating the catastrophe: magnetic configuration

1.3) Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

1.5) Is there a catastrophe or was there a catastrophe?

## 2) Fragmentation crisis2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

#### Influence of a weak magnetic field on the fragmentation

µ=1000 (hydro)

μ=50

#### μ=20



### **Influence of a weak magnetic field on the fragmentation** $\mu$ =1000 (hydro) $\mu$ =50 $\mu$ =20



#### For smaller $\mu$ , magnetic braking removes the disk

μ=2

μ=5

µ=1.25



Sonntag, 21. Oktober 12

#### For smaller $\mu$ , magnetic braking removes the disk

μ=2

µ=1.25





Sonntag, 21. Oktober 12

μ=5

Fragmentation: results of Machida et al. 2005



Observations (Crutcher 2004, Goodman et al. 1993, Caselli et al. 2002)

μ<5 (may be <2) β<0.07 (β=0.02, typical)

Hennebelle & Teyssier 2008 amplitude of perturbation: 0.1  $\mu$ : 1000-1.25 corrected  $\beta$  about 0.01 (uncorrected  $\beta$  =0.045)

> No class-0 disk Class-0 disk no fragmentation Fragmentation

$$\Omega_{c} / (4\pi G\rho_{c})^{1/2} = \sqrt{\beta}, \quad \beta = E_{rot} / E_{grav}$$

$$B_{zc} / (8\pi C_{s}^{2}\rho_{c}) \approx \sqrt{3} / (\sqrt{\alpha}\mu), \quad \alpha = E_{therm} / E_{grav}, \mu = (M/\phi) / (M/\phi)_{crit}$$

#### Why magnetic field stabilizes the disk so efficiently ?

Consider a uniformly rotating, self-gravitating, magnetized layer. Lynden-Bell (1966) obtained the dispersion relation:

$$\omega^{4} - \left[ 4\Omega^{2} - 2\pi G\Sigma_{p}|k| + k^{2} \left( c^{2} + \frac{B^{2}}{4\pi\rho} \right) \right] \omega^{2} + \frac{\left(k^{2} c^{2} - 2\pi G\Sigma_{p}|k|\right)(\mathbf{k}, \mathbf{B})^{2}}{4\pi\rho} = 0$$

(1)

It entails a modified sound speed due to the magnetic pressure forces => stabilizing effect.

But destabilizing contribution of the magnetic tension ⇒Configuration unstable

However, in a differentially rotating system (like a disk in Keplerian rotation), a toroidal magnetic field is quickly generated and the first effect becomes dominant. (Elmegreen 1987, Gammie 1996) Amplitude of the disk response for various Q, in presence of shear



When the Alfven speed within the disk is comparable to the sound speed, the response to a perturbation is much weaker.

Can we use this criteria to understand more quantitatively the numerical results ?

## Growth of the toroidal

magnetic field within the disk

Importance of  $V_a/C_s$ 



=>Compatible with the assumption that the toroidal field, stabilizes the disk.



Catastrophic braking
 1.1) The catastrophe...

1.2) Alleviating the catastrophe: magnetic configuration

**1.3)** Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

## 2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

#### 2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

## **Influence of non-ideal MHD**

## Ambipolar diffusion

#### Duffin & Pudritz 09 A fastly rotating model



## Ohmic dissipation

Machida + 08 147 simulations treating 2<sup>nd</sup> collapse 102 simulations fragment Simulations with realistic initial conditions fragment only during the second collapse





m=2 perturbation with an amplitude of 50%



Sonntag, 21. Oktober 12



Catastrophic braking
 1.1) The catastrophe...

1.2) Alleviating the catastrophe: magnetic configuration

**1.3)** Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

## 2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

#### 2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

### 100 $M_{\odot}$ magnetized, turbulent and dense barotropic core

#### (other related works : Peters et al. 2010, Seifried et al. 2012)

Turbulance is initially acceled Eturb / Eans. 000/



Hennebelle et al. 2011

Catastrophic braking
 1.1) The catastrophe...

**1.2)** Alleviating the catastrophe: magnetic configuration

1.3) Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

### 2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

#### 2.4) When magnetic field and radiative feedback collaborate

2.5) A crisis: really ?

#### 100 $M_{\odot}$ turbulent dense core collapse

#### Eturb/Egrav=20% initially



Commerçon, Hennebelle & Henning, ApJL 2011

(see also Price & Bate 2009 at larger scales)

#### $100 \ M_{\odot} \ turbulent \ dense \ core \ collapse$



#### $100 \ M_{\odot} \ turbulent \ dense \ core \ collapse$



*Commerçon, Hennebelle & Henning, ApJL* 2011

#### $100 \ M_{\odot} \ turbulent \ dense \ core \ collapse$



*Commerçon, Hennebelle & Henning, ApJL* 2011

Catastrophic braking
 1.1) The catastrophe...

**1.2)** Alleviating the catastrophe: magnetic configuration

**1.3)** Alleviating the catastrophe: impact of turbulence

1.4) Alleviating the catastrophe: non-ideal MHD ?

**1.5)** Is there a catastrophe or was there a catastrophe?

### 2) Fragmentation crisis

2.1) A fragmentation "crisis" for low mass cores ?

2.2) How to solve it ?

2.3) Influence of B on high mass cores

2.4) When magnetic field and radiative feedback collaborate

#### 2.5) A crisis: really ?

### **Confrontation with real observations of massive class-0 cores** Palau et al. 2013

Some cores show sign of fragmentation some not. No obvious correlation with any observed parameters (mass, rotation...). Magnetic field ?



Sonntag, 21. Oktober 12

## **Conclusions regarding fragmentation**

In low mass cores, the magnetic field has a huge impact on the fragmentation, especially "rotationally driven fragmentation"

-"large scale fragmentation" induced by initial large scale density perturbations is possible

-"small scale fragmentation" during second collapse is possible even when the field is strong

In high mass core, the magnetic field reduces but do not suppress fragmentation because the magnetic field is diffused out

The combination of magnetic field and radiative feedback leads to a very significant quenching of fragmentation. Route to form massive stars ?