Evolution of the Turbulent Interstellar Medium in Star Forming Galaxies

Dieter Breitschwerdt



Zentrum für Astronomie und Astrophysik Technische Universität Berlin



Collaborators

Miguel de Avillez (Evora, Portugal)
 + Research group at TU Berlin



- Introduction
- Interstellar Turbulence
- * 3D High Resolution Numerical ISM Simulations
- * Non-Equilibrium Ionization Structure of the ISM
 - Time and Space dependent Cooling Function
- Comparison to Observations
 - OVI (FUSE data), n_e (Pulsar dispersion measures)

Summary & Conclusions





Dieter Breitschwerdt (TU Berlín) - ISM Workshop Göttingen, 9.10.2012

Textbook ISM:

 $(f_{vh} > 50\%)$

Observations:

ture on all scales

 \rightarrow turbulence

30%)

• gas resides in distinct

smooth *stable* phases

hot phase has large

volume filling factor

• phase transitions in

pressure equilibrium

• filaments, frothy at

high resolution; struc-

• wide range of tempe-

ratures, densities (f_{vh} <

• gas, magnetic fields,

cosmic rays, dust ...

 \rightarrow multicomponent

Interstellar Turbulence

- * **Reynolds Number** is high: $Re = u L/v \sim 3 \ 10^3 M L [pc] n [cm^{-3}]$, i.e. $10^5 10^7$ (Elemegreen & Scalo, 2004); M = u/c ... Mach number
- * ISM is highly turbulent and compressible! (v. Weizsäcker 1951)

* Possible driving sources:

- * stellar: HII regions, stellar winds, supernovae (SNe), superbubbles
- * galactic differential rotation
- * <u>self-gravity</u>: Jeans instability, thermal instability
- * *plasma instabilities*: Rayleigh-Taylor, Kelvin-Helmholtz, magnetorotational instability (MRI), cosmic ray streaming etc.
- SNe dominate energy input in spirals (MacLow & Klessen 2004):



Turbulence I

- Reynolds-number: Re=u L/v ~ 10^5 10^7 *
- Nonlinearity $(u\nabla)u$ in Navier-Stokes-Eq. *

$$\frac{\partial \vec{u}}{\partial t} + (\vec{u} \nabla) \vec{u} = -\nabla \left(\frac{P}{\rho}\right) + \nu \nabla^2 \vec{u}, \, \vec{\omega} = \nabla \times \vec{u}$$

take curl and write as a function of vorticity ω :

$$7(\frac{1}{2}u^2) = (\vec{u}\nabla)\vec{u} + \vec{u} \times \vec{\omega}, \quad \frac{\partial\vec{\omega}}{\partial t} = \nabla \times [\vec{u} \times \vec{\omega}] + \nu\Delta\vec{\omega}$$

and since

$$\nabla \times [\vec{u} \times \vec{\omega}] = (\vec{\omega} \cdot \nabla)\vec{u} - (\vec{u} \cdot \nabla)\vec{\omega}$$

we have

$$\frac{D\vec{\omega}}{Dt} \equiv \frac{\partial\vec{\omega}}{\partial t} + (\vec{u}\cdot\nabla)\vec{\omega} = (\vec{\omega}\cdot\nabla)\vec{u} + \nu\Delta\vec{\omega}$$

change of moment of inertia by Change of stretching of fluid element (b) vorticity:



Incompressible

Newtonian fluid





laminare Strömung

turbulente Strömung

Strömungsrichtung

Turbulence II

• **Turbulence**: essentially a 3D chaotic solution of NS-Eq., but has large number of degrees of freedom

Stretching of fluid elements causes increase in vorticity

→ "vortex tubes"





Large Eddy Simulation of isotropic turbulence in a periodic box; shown are contours of vorticity



Direct Numerical Simulation of isotropic turbulence (s.a.); Re ~1200 (cf. Davidson)

3D-Simuation of a laboratory jet in non-reactive gas, Re ~21000 (2D projection) Credit: D. Glaze (Purdue University); arrows: velocity field

Turbulence III

- * Turbulence model: Kolmogorov (1941, K41), for <u>incompressible</u> turbulence (∇u=0)
- * Assumptions for large Re:
- (i) turbulence on small scales is
 <u>statistically isotropic</u> → universal
- * (ii) statistics on small scales is exclusively determined by v and $\varepsilon_D = \frac{\varrho u^2}{\tau}$ (**dissipation**)
- Richardson: energy cascade from large to small eddies
- * Large eddies generated by instability →
 break-up into smaller eddies → kin. energy
 rate per unit mass ε_K=u²/τ= u³/l=const.
 ("turn-over time": τ=l/u) → u ~ l^{1/3} (Q~const.) *
- ★ → observed in clouds: $\sigma \sim L^{0.38}$ (Larson, 1981)
- Energy input on large scales; cascade driven by inertial forces, viscous stresses negligible for large eddies ("inertial range")

Dieter Breitschwerdt (TU Berlín) - ISM Workshop Göttingen, 9.10.2012



Spectral energy density E(k) in Kolmogorov turbulence

Energy dissipation on micro-scale η → viscous forces dominate: Re=uη/ν ~ ~ (ε_K/ϱ)^{1/3} η^{4/3}/ν ~1 → η ~ (ν³/ε_K)^{1/4}

•
$$u \equiv v \sim v/\eta = (v \varepsilon_K)^{1/4}$$

* Energy dissipation rate $\varepsilon_D = \varepsilon_K$, independent of Re and l! $1/2 < u_i u_i > = \int E(k) dk$

Dimensiononal analysis:

- [k]=1/L, [E(k)]=L³ T⁻², [ϵ_D]=L² T⁻³ (iii) **E(k) = f(k,\epsilon_D) = C \epsilon_D^{2/3} k^{-5/3}**
- C is a universal constant!
- * structure function (of order n): $\langle [\delta \mathbf{u}(r)]^n \rangle = C_n \varepsilon^{n/3} r^{n/3}$

Turbulence IV

- Compressible Turbulence model: v.Weizsäcker
 (1951), Fleck (1996)
- Assumptions:
- (i) no magnetic field
- (ii) no self-gravity
- (iii) scale-invariant density fluctuations
 ("clouds") obey a hierarchy of scales on subsequent levels v:

$$\frac{\rho_{\nu}}{\rho_{\nu-1}} = \left(\frac{l_{\nu}}{l_{\nu-1}}\right)^{-3\alpha}, \ 0 \le \alpha \le 1$$

 $0 \le \alpha \le 1$: compressibility, $\varrho_v \dots$ average density, $3\alpha \dots$ number of dimensions for compression

- (iv) α essentially the **same** on all levels

$$\frac{1}{10^{-2}} = \frac{1}{10^{-2}} = \frac{1}{10^{-2$$

Spectra of v and u for compressible and incompressible (MHD) turbulence (Kowal & Lazarian 2007); α =0.23 \rightarrow k^{5/3} E(k) ~ k^{-2\alpha} ~ k^{-0.46}

Set of scaling relations:

$$\rho \sim l^{-3\alpha}, N \sim l^{1-3\alpha}$$
$$M \sim l^{3-3\alpha}, u \sim l^{1/3+\alpha}$$
$$E(k) = \frac{1}{2} \frac{dv^2}{dk} \sim k^{-5/3-2\alpha}$$

- fractal dimension: D=3-3α
- transformation to K41 (v~l^{1/3}) by
 v=Q^{1/3} u (density weighted velocity, *Kritsuk et al.* 2007) → restoring the 2nd order velocity structure function
- * α=0.15 (*Kritsuk et al.* 2007)

 $\rightarrow o^{1/3} u \sim l^{1/3} \equiv v$



ISM Simulations I: Large Scales

- Goal: simulate whole galaxies
- * **3D SPH** (Dobbs et al. 2011)
- fixed gravitational potential, including spiral arms
- heating & cooling, self-gravity
- no magnetic fields
- energy source due to star formation
 (SF), efficiency 5 40%
- UV photon background field
- maximum mass resolution: 2500
 M_{sol} (larger than Jeans length)
- focus on clouds, cold gas
- for T>5000 K, n ~ 10⁻³ cm⁻³: Δl ~ 300 pc: too large for studying turbulence and gas phase transitions



Evolution of column density (Dobbs et al. 2011, MNRAS; courtesy Claire Dobbs)

ISM: Numerical Simulations II

- * **Mesoscale ISM simulations**: sufficiently large to cover integral scale, sufficiently small to resolve gas phases distributions ($\Delta x=0.5$ pc or less)
- * Solve full 3D HD/MHD equations on a large grid: 1 kpc × 1 kpc × ± 10 kpc
- * Type Ia,b,c/II Supernovae random + clustered in disk
- * Background heating due to diffuse UV photon field (Wolfire et al. 1995)
- * Thermal conduction including saturation (Dalton & Balbus 1993)
- Gravitational field by stars + self-gravity
- * SFR \propto local density/temp.: n >10 cm⁻³/T<100 K
- * Generate stars according to an IMF
- ★ Formation and motion of OB associations (→ random velocity of stars)
- * Fully time-dependent **non-equilibrium ionization (NEI) structure**
- * Evolution of computational volume for $\tau \sim 400 \text{ My}$
- ★ → sufficiently long to erase memory of initial conditions!
- * 3D calculations on parallel processors with adaptive mesh refinement (AMR) grid code *Dieter Breitschwerdt* (*T'U Berlin*) - 1SM Workshop Göttingen, 9.10.2012

HD-Evolution of ISM

Collective effect of SNe induces break-out of ISM disk gas → "galactic fountain" (cf. intermediate velocity clouds) → reduce disk pressure y

- Density and temperature distribution shows structures on all scales (cf. observation of filaments)
- shear flow due to expanding SNRs generates high level of turbulence → coupling of scales
- Cloud formation by shock compressed layers → clouds are transient features → generation of new stars
- large amount of gas in thermally unstable phases
- volume filling factor of HIM ~ 20%
- no pressure equilibrium!





2D cuts through 3D data cube (disk cut)



Dieter Breitschwerdt (TU Berlin) - ISM Workshop Göttingen, 9.10.2012

Results

- * Pressure far from uniform: spatial variation even for high SN rate ($\sigma/\sigma_{gal} = 4$)
- <P/k> ~ 3000 for Milky Way, i.e. less than canonical values of > 10,000
- Reason: due to fountain flow, average disk pressure can be lowered
- lots of small scale structure: filaments
- ★ shock compressed layers → cloud formation
- ★ lower volume filling factor for HIM: f_V ~ 0.2
- * lots of gas in thermally unstable regions

Results II: Volume filling factors

σ/σ_g	f _{cold}	f_{cool}	f _{warm}	f _{hot}
1	0.19	0.39	0.25	0.17
2	0.16	0.34	0.31	0.19
4	0.05	0.3	0.37	0.28
8	0.01	0.12	0.52	0.35
16	0	0.02	0.54	0.44

cold: T<10³ K; cool: $10^3 <$ T< 10^4 K warm: $10^4 <$ T< $10^{5.5}$ K; hot: T>10^{5.5} K

- increase in SN rate:
- * f_V of hot gas still not dominating!
- f_V of cold gas decreases substantially



- f_V fairly const. with time for t > 200 Myr
- Reason: break-out of SBs and galactic fountain flow acts as pressure release valve!
- f_V of hot gas is fairly low!
- in agreement with HI holes in external galaxies

Results III: Probability Density Functions (PDFs) Avillez & Breitschwerdt, 2009



- * PDF gives probability to find a fraction f(x) of gas in given density / pressure regime
 * For X∈ {Q,P}) we have: P(a ≤ X ≤ b) = ∫^b f(x)dx
- In a SN driven ISM the distribution is very broad → substantial fraction of gas exists outside "phases", i.e. in thermally unstable regions!

MHD-Evolution of ISM I







Outflow not inhibited by B-Field; lines of force drawn out by disk-halo flow → loop structure Dieter Breitschwerdt (T'U Berlin) - ISM Workshop Göttingen, 9.10.2012



MHD-Evolution of ISM II

221.90 My

Avillez & Breitschwerdt, 2005a

B-field / / to disk cannot prevent outflow into halo; Halo density is **inhomogeneous (Fountain)**



Which pressure determines ISM dynamics?
For T < 200 K: magnetic pressure dominates,
for 200 K < T < 10⁶ K ram pressure dominates,
for T>10⁶ K thermal pressure dominates Dieter Breitschwerdt (TⁱU Berlin) - 1SM Workshop Göttingen, 9.10.2012



Stability of "Phases" (I)

- * Heiles (2001) reports that > 47% of WNM is in a classically unstable phase between 500 – 5000 K
- * Our simulations show that in total 40% of ISM mass is unstable
 - * 500 < T < 5000 K: ~ 55% of the gas is unstable
 - * $T > 10^{5.5}$ K: ~10% is unstable
- * Does this contradict classical thermal stability theory (Field, 1965)?
- Not necessarily, because
 - * stability of "phases" was derived in a time-asymptotic limit:
 - * instability means that cooling time << dynamical time scale</p>
 - * stable points determined by properties of interstellar cooling curve
- * However, in a time-dependent dynamical picture things can be different (e.g. Kritsuk & Norman 2002, Gazol et al. 2001)
 - * SN increased **turbulence** can work against condensation → turbulent transport of energy (cf. heat conduction in the solar chromosphere)
 - * eddy crossing time << cooling time</p>

Stability of "Phases" II

- * Field criterion does not take into account turbulent dynamics
- Turbulent diffusion can stabilize, inhibiting local condensation modes (cf. solar chromosphere), transporting energy to cooling regions: v_{turb} ~ Re v_{mol}
- * Thermal instability inhibited, if fluctuations occur on time scales less than the cooling time: $\tau_{eddy} << \tau_{cool}$

$$\tau_{\text{eddy}} \sim \frac{\lambda}{\Delta u} \sim \left(\frac{\rho}{\epsilon}\right)^{1/3} \lambda^{2/3} < \frac{k_B T}{n\Lambda(T)}$$
$$\Rightarrow \lambda < \left(\frac{k_B \bar{m}}{\Lambda_0}\right)^{3/2} \frac{\epsilon^{1/2}}{\rho^2} T^{3/4}, \Lambda(T) = \Lambda_0 T^{1/2}$$

(incompressible turbulence)

- * values for WNM: $\varepsilon \sim 10^{-26}$ erg cm⁻³ s⁻¹, n~0.3 cm⁻³, T~1000 K, $\Lambda_0 \approx 1.9 \ 10^{-27}$ erg cm³ s⁻¹ K^{-1/2}: $\lambda < 10^{19}$ cm \rightarrow thermal instability inhibited on parsec scales
- * compressible turbulence: strong dependence on α in "Fleck-model":

$$\lambda < \left[\frac{3}{2} \left(\frac{\epsilon_V}{\rho_0^4}\right)^{1/3} \frac{\bar{m}k_B T^{1/2}}{\Lambda_0} l_0^{-4\alpha}\right]^{3/(2-12\alpha)}$$
(compressible turbulence)

* compressibility decreases critical length, because cooling time decreases faster than turn-over time; $\alpha \sim 0.1$: $\lambda \sim l_0^{-0.4} T^{1.75}$; $\alpha = 0$: $\lambda \sim T^{0.75}$

Stability of "Phases" III

- * WNM in the thermally unstable temperature regime (500 - 1500 K) shows filamentary structure
- classically there should be no (or only very little) gas observable!!!
- distribution on small scales (~ pc)
- ★ → agreement with HI observations by Heiles (2001), Heiles & Troland (2003)



WNM in the thermally unstable regime: $631 \text{ K} \le \text{T} \le 1585 \text{ K}$

At which scale is turbulence generated? $= \frac{B_{mean} = 3\mu G}{B_{mean} = 2\mu G}$

- ★ ISM turbulence is generated by shear flows → increases vorticity
- * largest eddies break up at a turn-over time $\tau \sim l/\Delta v \rightarrow$ energy fed in at large scale
- Richardson (1922):
 "Big whorls have little whorls that feed on their velocity, and little whorls have lesser whorls and so on to viscosity"
- * 2nd order structure function (measure for E_{kin} contained in eddie of size r)
 S₂(r) = ⟨(Δv)²⟩ = ⟨[u_x(x + rē_x) u_x(x]]²⟩
 * integral scale ~ break-up scale of

superbubbles



 $\langle S_2(r) \rangle$ flattens at r ~ 75 pc: integral scale Fleck (1996): $S_p(r) \sim v^p \sim l^{p/3} \rightarrow S_2(r) \sim l^{2/3}$

 $\frac{1}{2}\left\langle \vec{u}^{2}\right\rangle =\int_{0}^{\infty}E(k)dk\,, \frac{1}{2}\left\langle \vec{\omega}^{2}\right\rangle =\int_{0}^{\infty}k^{2}E(k)dk$

Non-equilibrium ionization (NEI) structure of ISM (I)

- optically thin hot plasmas: continuum + line spectrum (n_e < 10⁴ K: coronal approx.)
- * collisional ionization equilibrium (CIE): ionization by collisions (3-body process) is balanced by radiative recombination → no detailed balancing, because atomic time scales are different
- plasma is driven out of CIE → non-equilibium ionization (NEI) structure, e.g.
 Kafatos (1973), Shapiro & Moore (1976),
 Stone & Norman (1993) etc.
- particularly striking effect: fast adiabatic cooling like in a galactic fountain or wind (Breitschwerdt & Schmutzler, 1994)





radiative recombination



Top: CIE vs. NEI plasma emission codes; in **CIE**, plasma emission can be calculated (in coronal approx., i.e. $n_e < 10^4$ cm⁻³) once and for all if n_e , T_e and Z are given; in **NEI** Z + astrophysical model for dynamical evolution is required! **Left:** Animation of collisional ionization by electrons

Dieter Breitschwerdt (TU Berlin) - ISM Workshop Göttingen, 9.10.2012

Example: ionization structure of oxygen in CIE and NEI



- ★ CIE: ionization fractions x of O depend only on temperature T (for given Z)
 → sharply peaked → convenient diagnostic tool for determining T
- * NEI: *x* depends on dynamical and thermal history of plasma → more difficult to fit spectrum, but: evolution of plasma can (in principle) be inferred!

NEI structure of ISM (II)

Avillez, Breitschwerdt, Manuel (2011)

- Flow changes **e** and **T**
- this modifies ionization structure
- which in turn modifies cooling function
 Λ(T,Z)
- which changes outflow
- ★ Time-dependent Cooling Function
- Modelling: use 10 most abundant elements
- 3D hydrodynamics (parallelized with AMR) with a highest resolution of 0.5 pc
- include most important processes: electron impact ionization, excitation auto-ionization, radiative and dielectronic recombination, charge exchange reactions, continuum (bremsstrahlung, free-bound, 2-photon) and line emission



Top: 3D high resolution NEI simulation, cut through galactic midplane (at solar circle), after evolution time t= 400 Myr

NEI structure of ISM (III)

- CIE cooling curves are no longer valid → cooling depends on the **thermal** and **dynamical history** of the plasma, i.e. distribution of ionization stages
- Ionization structure varies from place to place and with time \rightarrow multitude of different cooling functions: $\Lambda = \Lambda(\mathbf{r},\mathbf{t}; \mathbf{T}, \mathbf{Z})$
- delayed ionization: plasma is *underionized* due to slow ionization of neutral plasma → typical for cold plasmas collisionally ionized by shocks
- delayed recombination: plasma is *overionized* due to slow recomb. of high ionization stages → typical for very hot cooling plasmas
- NEI cooling curves of cooling down plasma below CIE since deficiency of outer electrons for line emission
- X-ray observations of diffuse hot plasma show signs of delayed recombination

Dieter Breitschwerdt (TU Berlin) - ISM Workshop Göttingen, 9.10.2012



Top: Midplane cut of NEI simulations marking regions of
different temperatures: 10^{5.5} K (F-J), 10⁶ K (K-O)Bottom: Cooling curves of different places with different
initial temperatures; dotted line is CIE and and dashed line
is NEI of an initially completely ionized plasma46

NEI structure of ISM (IV)

* NEI spectrum:

- saw-tooth emission line structure
- soft X-ray emission at kinetic temperatures as low as 25,000 K!!!
- NEI emission at 0.3 keV higher at T=10⁴ K than CIE emission at 10⁶ K
- * CIE emission at 0.3 keV for T=10⁴ K negligible
- NEI spectrum unique, as it reflects the thermal and dynamical history of the plasma



Top: NEI simulation of free-bound emission of a plasma initially at temperature 10⁶ K located at sites K-O

Modeling soft X-ray emission from the ISM

Procedure:

- Generating an ISM model and follow time-dependent evolution of ions (NEI) → integrate spectrum along line of sight
- Binning of high-resolution unabsorbed synthetic (model) spectrum into e.g. EPIC pn channels (for XMM-Newton)
- * Folding spectrum through detector response matrix

Treating observed and synthetic spectrum equally! (Breitschwerdt 2003)

- Fitting synthetic spectrum in XSPEC (X-ray spectral fitting routine) to observational data
- * **Comparing** with observed spectrum and iterate outflow model if necessary until convergence



Comparison to Observations I: OVI



- OVI traces cooling down HIM
- OVI produced in turbulent mixing layers!
- **70%** of OVI in **NEI** below 10⁵ K,
 i.e. well below the CIE value!!!



- OVI temperature distribution in the ISM; shown are values $10^{3.8} < T(OVI) < 10^{6.1}$ K highest n(OVI) densities in cool clumpy regions
- Zoom into bubble shows turbulent mixing

Comparison to Observations II: OVI

- FUSE & Copernicus data of OVI absorption lines towards background stars
- Comparison with NEI simulations: spatially averaged (red and blue curves) and single LOS of N(OVI) at different angles and at different times
- N(OVI) converges to an average value of 1.3 - 1.4 10⁻⁸ cm⁻²
- ★ FUSE observations for |z| ≤ 150 pc: N(OVI) ~ 1.3 10⁻⁸ cm⁻² (Bowen et al. 2008)
- dispersion of N(OVI) ~ const. \rightarrow clumpy distribution along LOS



N(OVI) density in the ISM as a function of LOS

Comparison to Observations III: Electron distribution

- Study electron density distribution n_e in solar neighbourhood in NEI
- Simulations in good agreement with **pulsar dispersion measures** (DM= $\int n_e dl$) for $|b| < 5^\circ$; $< n_e > = DM/d$
- * n_e distribution is **lognormal**: $< n_e > = 0.04 \pm 0.01$ cm⁻³
- Reason: Maximum entropy principle, central limit theorem



NEI-Model





Avillez, Asgekar, Breitschwerdt, Spitoni (2012)

Top: NEI simulation of electron density **Left:** Electron density derived from measurements of 75 pulsars for |z| < 200 pc, with 200 pc < d < 8 kpc; Result: $\log(n_e) =$ -1.47 ± 0.02 , $\sigma = 0.17 \pm 0.02$ **Right:** Histograms (solid line) and Gaussian fits (dashed line) from dispersion measures of <u>NEI</u> <u>simulations</u> taken at different times from 350 -400 Myr; $\log(n_e) = -1.4$ to -1.38, $\sigma = 0.16 - 0.21$

Comparison to Observations IV: Electron distribution

- Electron distribution n_e is different for NEI, as the ionization structure, and hence the number of free electrons is different
- Pulsar dispersion measures (mean, minimum and maximum) are in good agreement with observations (from ATNF catalogue with distance measurements)
- n_e remains almost constant with distance
- 80% of n_e by mass in thermally unstable region (200 < T < 10^{3.9}); WNM filling factor 4-5% (Gaensler et al. 2008)





Top: NEI simulation of gas density (including Local Bubble and Loop I)

Left: time averaged dispersion measures (mean, minimum and maximum) over a period of 50 Myr, 501 snapshots taken at 0.1 Myr intervals Right: electron density as a

function of distance (blue crosses: pulsar observations)

Summary

- * ISM is a highly turbulent, compressible medium → nonlinear dynamics requires high resolution numerical simulations
- * Simulations require:
 - * (i) sufficiently long evolution time to erase "memory" effects of initial conditions
 - (ii) inclusion of essential physical processes; still missing: detailed chemistry, radiation transport, cosmic rays, differential rotation, galactic dynamo ...
 - * (iii) observables should be independent of resolution
- * SN-driven ISM shows structures on **all scales** (coupling by **turbulence**)
- * High level of turbulence maintained by on-going **star formation**
- "Galactic Fountain" acts as pressure release valve in the disk → reduces volume filling factor of hot "phase"
- * ISM **not** in pressure equilibrium (average pressure lower in agreement with observation)
- * "Clouds" are shock compressed layers, in which new stars are born
- * Large mass fraction in **thermally unstable** regime
- OVI-distribution due to turbulent mixing → in good agreement with FUSE- and Copernicus data
- Dynamical and turbulent ISM drives plasma out of ionization equilibrium (NEI) → interstellar cooling function depends on plasma history and hence varies in space and time
- Electron density distribution lognormal (n_e=0.04±0.01 cm⁻³) consistent with pulsar obs.
- * Closest to Earth SN: ~ 2.2 Myr. at ~ 85 pc distance (derived from fit to ⁶⁰Fe data)

Thank you for your attention!

